Soil water / Unsaturated Zone Hydrology



Paperback | 351 pages Follow the book's didactic concept!

- Hydrological cycle
- Drainage basin
- Water balance
- Energy equation
- Flow equation
- Continuity equation
- 1. Introduction
- 2. Atmospheric water
- 3. Groundwater
- 4. Soil water
- 5. Surface water

Exercises

Infiltration capacity

Ponded infiltration



Infiltration envelope



Horton equation

Ponded infiltration

$$f_{t} = f_{c} + (f_{0} - f_{c}) e^{-\alpha t}; f_{t} - f_{c} = (f_{0} - f_{c}) e^{-\alpha t}$$

$$f_{t+\Delta t} - f_{c} = (f_{0} - f_{c}) e^{-\alpha (t+\Delta t)} = (f_{0} - f_{c}) e^{-\alpha t} e^{-\alpha \Delta t} = (f_{t} - f_{c}) e^{-\alpha \Delta t}$$

$$f_{t+2\Delta t} - f_{c} = (f_{0} - f_{c}) e^{-\alpha (t+2\Delta t)} = (f_{0} - f_{c}) e^{-\alpha t} e^{-2\alpha \Delta t} = (f_{t} - f_{c}) (e^{-\alpha \Delta t})^{2}$$

$$f_{t+\frac{1}{2}\Delta t} - f_{c} = (f_{0} - f_{c}) e^{-\alpha (t+\frac{1}{2}\Delta t)} = (f_{0} - f_{c}) e^{-\alpha t} e^{-\frac{1}{2}\alpha \Delta t} = (f_{t} - f_{c}) (e^{-\alpha \Delta t})^{\frac{1}{2}}$$

$$f_{t} - f_{c} \text{ at } t = t_{1}$$

$$f_{t} - f_{c} \text{ at } t = t_{2}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

$$f_{t} - f_{c} \text{ at } t = t_{3}$$

Two different values of α

Ponded infiltration



Philip equation

Ponded infiltration



For t = 1 minute: $f = \frac{1}{2}S + K$

For t = 1 minute: F = S + K

Philip equation

Estimate the values of S and K_s

 $i = \frac{1}{2}St^{-0.5} + A$



$$\frac{0.40 - 0.12}{0.5 - 0.1} = \frac{0.28}{0.4} = 0.7 \text{ mm s}^{-0.5}; \text{ the slope} = \frac{1}{2}S$$

S is twice the slope = 1.4 mm s^{-0.5}

Intercept with the *i*-axis: 0.05 mm s⁻¹

$$K_{\rm s} = \frac{3}{2}A = 0.075\,{\rm mm~s^{-1}} = 6.48\,{\rm m~day^{-1}}$$

Texture: sand

Estimation of the sorptivity S



The horizontal water flow is mainly controlled by capillary action!

$$F = S\sqrt{t}$$
 and $F = L(\theta_{\rm s} - \theta_{\rm i})$

Non-ponding infiltration

Potential diagram



Evaporation and percolation

Potential diagram



Development of zero flux planes



Adapted from Wellings and Bell (1982)



Effect of soil layering on percolation



Profiles of the change with time (hours) of volumetric moisture content (a) and matric potential (b) during a constant rate of water application to a layered soil (after Vachaud et al. 1973)

Fingered flow due to soil heterogeneity

toplayer fine soil ⇔ sublayer coarse soil
high capillary suction ⇔ low capillary suction
low conductivity ⇔ high conductivity



Fingered flow due to soil heterogeneity



Unsaturated flow

Traditionally :

- uniform
- vertical flow
- Richards equation



Preferential flow !!!





Preferential flow

Macropore flow

Fingered flow



Funnel flow

Source: Cornell University Soil and Water Laboratory



Exercise 4.9



Taking the soil as homogeneous can lead to a strong underestimation of the maximum depth of infiltration under high rainfall intensities!



References

Cornell University Soil and Water Laboratory: http://soilandwater.bee.cornell.edu/Research/pfweb/

Hendriks, M.R. (2010). Introduction to Physical Hydrology. Oxford University Press.

Horton R.E. (1939). Analysis of runoff-plot experiments with varying infiltration capacity. Transactions, American Geophysical Union, 20, 693–711.

Vachaud, G., Vauclin, M., Khanji, D. and Wakil, M. (1973). Effects of air pressure on water flow in an unsaturated stratified vertical column of soil. Water Resources Research, 9, 160-173.

Wellings, S.R. and Bell, J.P. (1982). Physical controls of water movement in the unsaturated zone. Quarterly Journal of Engineering Geology, 15(3), 235-241.